- (a) What do you understand by a control chart? Give justification for using the 3cr control limits in the control charts.
  - (b) In order to determine whether or not a production of bronze casting is in control, 20 sub-groups of size 6 are taken. It is found that  $\overline{\overline{x}} = 3.126$  gm; and  $\overline{R} = 0.009$  gm. Assuming that the process is in control, find upper and lower control limits for the sub-groups' means and ranges. (6,6)
- (a) Define process and product control. Give justification for using 3σ control limits in the control charts.
  - (b) Explain the construction of p and d- charts. Also, discuss the construction of control limits of p and d-charts for fixed and variable sample sizes.
  - (c) The following are the numbers of defectives in 22 lots each containing 2,000 rubber belts :

425	430	216	341	225	322	280	306	337	305	356
402	216	264	126	409	193	326	280	389	451	420

Draw control chart for fraction defectives and comment on the state of control of the process. (4,4,4)

(1000)

[This question paper contains 6 printed pages.]

Sr. No. of Question Paper :6229EUnique Paper Code:32375902Name of the Paper:Applied StatisticsName of the Course:Generic Elective: StatisticsSemester:IVDuration : 3 HoursMaximum Marks : 75

Your Roll No.....

## **Instructions for Candidates**

- 1. Write your Roll No. on the top immediately on receipt of this question paper.
- 2. Attempt six questions in all.
- 3. Question 1 is compulsory.
- 4. Select two questions from Section A and three from Section B.
- 5. Use of simple scientific calculator (non-programmable) is allowed.

Attempt any three parts :

- 1. (a) Define the following in context of a time series :
  - (i) Seasonal variation
  - (ii) Random component

P.T.O.

- (b) Define the following terms in relation to an index number :
  - (i) Price relatives
  - (ii) Quantity relatives
- (c) Differentiate between GRR and NRR. What are the main sources of errors while computing the GRR?
- (d) Explain how a control chart helps to control the quality of a manufactured product. Describe the construction of R-chart, when standard are not given.
  (3×5)

## Section A

2. (a) If L(p) and L(q) denote Laspeyre's price and quantity index numbers respectively; and P(p) and P(q) denote Paasche's price and quantity index numbers respectively. Then show that

$$\frac{L(p)}{L(q)} = \frac{P(p)}{P(q)}.$$

Also, show that if

$$A(p) = \frac{L(p) + P(p)}{2}$$

then  $A(p) \ge F(p)$ , where F(p) is Fisher's ideal index.

OR

Which Death rates reveal glaring facts about various segments of the population? Describe in detail giving its merits and demerits.

(c) Find the standardised death rate for the given data

Age	Standard	Population	Population A		
(Years)	Population ('000)	Specific Death Rate	Population ('000)	Specific Death Rate	
0-5	8	50	12	48	
5-15	10	15	13	14.	
15-50	27	10	15	9	
≥50	5	60	10	59	

(3,3,6)

- (a) What do you understand by Curate and Complete expectation of life? Show that (in the usual notations)
  - $\mathbf{e}_{\mathbf{x}}^{0} = \frac{\mathbf{T}_{\mathbf{x}}}{l_{\mathbf{x}}} \cdot$
  - (b) Describe a life table along with its assumptions and the steps required for the construction of the life table.
  - (c) Is Crude birth rate a probability ratio? Elaborate. (4,4,4)

P.T.O.

Commodity	Base year price (p <sub>0</sub> )	Base year quantity (q <sub>0</sub> )	Current year price (p1)	Current year quantity (q1)
A	1	6	3	5
В	3	5	8	5
C	4	8	10	6

(b) Verify the results of the above part for the following data set:

(6,6)

- (a) What do you understand by secular trend of a time series model? Name some methods to measure trend. Obtain normal equations for measuring trend if the trend can be measured by a straight line.
  - (b) Using the equations obtained in the above part, measure the straight line trend for the following data :

Time (t)	1	2	3	4	5	6	7
Production (Y)	77	88	94	85	91	98	90

(6, 6)

(a) On a certain date, the consumer price index for a certain class was 204.6. The percentage increase in the price in different categories over the base year are as follows :

P.T.O.

1 Caralitano	Parentage increase	Weight	
Class of expenditure	V	60	
Food	A	12	
Clothing	220	14	
Housing	65	10	
Tiousing	110	8	
Fuel and energy	125	4	
Miscellaneous	125	1	

Determine X.

- (b) Identify the components of a time series mainly applicable in the following cases citing appropriate reasons :
  - (i) Fire in a factory.
  - (ii) Stubble burning after the crop season is over.
  - (iii) Increasing population of a country.
  - (iv) Increasing digital literacy. (5,7)

## Section B

- 5. (a) Define Vital Statistics? How do you study Population trend and what is its significance?
  - (b) Define Rates and Ratios of Vital events. What is the significance of the sex-ratio? Also explain why C.D.R. is not suitable for comparing the mortality rates of two places?