$(1 \ 0 \ 1 \ 1 \ 1)$

Is it a totally ordered set? Justify your answer.

[This question paper contains 8 printed pages.]

		Four Kon No
Sr. No. of Question Paper	:	1216 F
Unique Paper Code	:	2342011202
Name of the Paper	:	Discrete Mathematical Structures
Name of the Course	:	B.Sc. (Hons.) Computer Science (NEP-UGCF-2022), 11001
Semester	:	II
Duration : 3 Hours		Maximum Marks : 90

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Instructions for Candidates

1. Write your Roll No. on the top immediately on receipt of this question paper.

2. Question No. 1 (Section-A) is compulsory.

3. Attempt any four questions from Section-B.

4. Parts of a question should be attempted together.

5. Use of simple calculator is allowed.

(1800)

(8)

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SECTION A

 (a) Determine whether the following function is oneto-one and onto from R⁺ to R⁺

$$f(x) = -3x^2 + 7$$

Also, check whether it is invertible. If invertible, find its inverse. Justify your answer in each case. (5)

- (b) Show that ¬(p∨(¬p ∧ q) and (¬p ∧ ¬q) are logically equivalent by developing a series of logical equivalences.
- (c) Evaluate 7⁶⁴⁴ mod 645 using Fast Modular exponentiation algorithm.
 (5)
- (d) Prove that if any 14 numbers from 1 to 25 are chosen then one of them will be the multiple of another.(5)

1216

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following pair of graphs are isomorphic. Give justification in support of your answer. (8)

7



- 7. (a) Is Q₃ a planar graph? If planar, draw it in such a form. Verily your result using Euler formula also. (7)
 - (b) Draw Hasse Diagram for the relation R on
 A = {1, 2, 3, 4, 5}, whose relation matrix is given below

6

(b) For the following numeric functions :

$$a_r = 2^r$$
 for all r

$$\mathbf{b}_{\mathbf{r}} = \begin{cases} 0 & 0 \le \mathbf{r} \le 2\\ 2^{\mathbf{r}} & \mathbf{r} \ge 3 \end{cases}$$

Determine a * b in either sketch or closed form expression.

- 6. (a) In how many ways can a cricket team of eleven be chosen out of a batch of 14 players? How many of them will:
 - (i) include a particular player?
 - (ii) exclude a particular player? (7)
 - (b) Define graph isomorphism. Check whether the

1216

(8)

(e) State whether the K_5 graph is/has a

3

- (i) Tree
- (ii) Euler Path
- (iii) Euler circuit
- Justify your answer.

(5)

(f) Let a be a numeric function such that (5)

- $a_{r} = \begin{cases} 2 & 0 \le r \le 3 \\ 2^{-r} + 5 & r \ge 4 \end{cases}$
- (i) Determine S^2a .
- (ii) Determine ∇a .

SECTION B

(a) Prove that the relation "congruence modulo m" over the set of positive integers is an equivalence relation. (7)

- (b) If no three diagonals of a convex decagon meet at the same point inside the decagon, into how many line segments are the diagonals divided by their intersections? (8)
- (a) Prove the following statement using the Direct 3. Proof method :

If m and n both are perfect squares, then m * n . 4 (7)is also a perfect square.

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- (b) Using the principle of mathematical induction, prove that
 - $1.2.3 + 2.3.4 + \cdots + n. (n + 1). (n + 2) = n(n + 1)$
 - (n + 2)/3(8)

1216

(a) Using the Euclidean algorithm, find the GCD of 4. 1529 and 14039. (7)

5

- (b) The interest for money deposited in a saving bank account is paid at a rate of 0.5% per month, with interest compounded monthly. \$50 is deposited in the saving account each month for a period of 3 years, followed by \$20 each month for next 2 years. What is the total amount in the account
 - (i) 4 years after the first deposit?
 - (ii) 20 years after the first deposit?
 - Formulate the numeric functions for each. (8)
- (a) Prove that a tree with n vertices has n 1 edges. 5.

(7)