

Name of Course : **CBCS (LOCF) Generic Elective- Mathematics**  
 Unique Paper Code : **32355101**  
 Name of Paper : **GE-1 Calculus**  
 Semester : **I**  
 Duration : **3 hours**  
 Maximum Marks : **75 Marks**

*Attempt any four questions. All questions carry equal marks.*

- Find the critical points, inflection points and asymptotes (if any) for the function  $f(x) = \frac{x^2+3}{x^2-4}$ . Determine the region where the function increase or decrease and also discuss its concavity. Also, sketch the curve.
- Evaluate the following limits using L'Hopital's rule  
 $\lim_{x \rightarrow b} \frac{x^b - b^x}{x^x - b^b}$  and  $\lim_{x \rightarrow \infty} [x - \ln(x^5 - 10^{10})]$ .
- Find the volume of the solid obtained by revolving the region bounded by the curves  $y = 2x^2 + 1$  and  $y = 3 - 2x^2$  about  $x$ -axis. Also find the length of the plane curve  $y = 2x^2 + 1$  over the interval  $[1, 3]$
- Sketch the graph of  $r^2 = \theta^2, 0 \leq \theta$  in polar coordinates.
- Let  $f(x, y) = \begin{cases} \frac{xy^n}{x^3+y^{3n}}, & (x, y) \neq (0, 0) \\ 0, & (x, y) = (0, 0) \end{cases}$  where  $n > 1$ .

Discuss the continuity of  $f(x, y)$ . And show that  $f_x(x, y)$  and  $f_y(x, y)$  exist at all points  $(x, y)$ .

- Find the equation of parabola which has axis parallel to  $y$ -axis and which passes through the points  $(0, 2)$ ,  $(-1, 0)$  and  $(1, 6)$ . And plot this parabola.  
 An ellipse circumscribes a rectangle whose sides are given by  $x = \pm 2$  and  $y = \pm 4$ . If the distance between the foci is  $4\sqrt{6}$  and major axis is along  $y$ -axis, then find the equation of the ellipse. Also, plot this ellipse.

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- If  $w = \ln(x^2 + y^2 + z^2)$ ,  $x = ue^v \sin u$ ,  $y = ue^v \cos u$  and  $z = ue^v$ , find  $\frac{\partial w}{\partial u}$  and  $\frac{\partial w}{\partial v}$  using chain rule at the point  $(u, v) = (-2, 0)$ .
- Find the directions in which the function  $f(x, y, z) = \ln xy + \ln yz + \ln xz$  increase and decrease most rapidly at the point  $P_0(1, 1, 1)$ . Then find the derivatives of the function in those directions.