

5. (a) Find the general solution of the differential equation : 6.5

$$x^2 p + y^2 q = (x + y)z.$$

- (b) Find the complete integral of the differential equation : 6.5

$$(p^2 + q^2)x^2 - qz = 0.$$

- (c) (i) Classify the partial differential equation as elliptic, parabolic or hyperbolic : 2.5

$$4u_{xx} - 4u_{xy} + 5u_{yy} = 0.$$

- (ii) Eliminate the parameters  $a$  and  $b$  from the following equation to find the corresponding partial differential equation : 4

$$z = x + ax^2y^2 + b.$$

6. (a) Find the complete integral of the equation : 6

$$(p + q)(z - xp - yq) = 1.$$

- (b) Eliminate the arbitrary function  $f$  from the equation  $z = x + y + f(xy)$  to find the corresponding partial differential equation. 6

- (c) Find the general solution of the partial differential equation : 6

$$y^2 p - xyq = x(z - 2y).$$

This question paper contains 4 printed pages]

Roll No. 

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S. No. of Question Paper : 1414

Unique Paper Code : 62357502

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Name of the Paper : Differential Equations

Name of the Course : B.A. (Prog.) Mathematics : DSE-2

Semester : V

Duration : 3 Hours

Maximum Marks : 75

(Write your Roll No. on the top immediately on receipt of this question paper.)

Attempt All the questions by selecting

any two parts from each question.

1. (a) Solve the initial value problem : 6

$$(3x^2y^4 + 2xy)dx + (2x^3y^3 - x^2)dy = 0; y(1) = 2,$$

- (b) Solve : 6

$$x = y + a \ln p.$$

- (c) Solve : 6

$$(y + x + 5)dy - (y - x + 1)dx = 0.$$

2. (a) Solve :

6.5

$$\frac{d^3 y}{dx^3} - 4 \frac{d^2 y}{dx^2} - 3 \frac{dy}{dx} + 18y = x.$$

(b) Solve :

6.5

$$(x+3)^2 \frac{d^2 y}{dx^2} - 4(x+3) \frac{dy}{dx} + 6y = x.$$

(c) Consider the following differential equation : 6.5

$$x^3 \frac{d^3 y}{dx^3} - 4x^2 \frac{d^2 y}{dx^2} + 8x \frac{dy}{dx} - 8y = 0$$

(i) Show that  $x$ ,  $x^2$  and  $x^4$  are solution of above differential equation.(ii) Show that the solutions  $x$ ,  $x^2$  and  $x^4$  are linearly independent.

(iii) Write the general solution of the above differential equation.

3. (a) Using the method of variation of parameters to find the general solution of : 6.5

$$\frac{d^2 y}{dx^2} + y = \tan x.$$

(b) Use the method of undetermined coefficients to find the general solution of the differential equation : 6.5

$$4 \frac{d^2 y}{dx^2} + 4 \frac{dy}{dx} + y = e^x + 2 \cos 2x.$$

(c) Given that  $y = x$  is a solution of the differential equation : 6.5

$$(x^2 + 1) \frac{d^2 y}{dx^2} - 2x \frac{dy}{dx} + 2y = 0.$$

Find a linearly independent solution by reducing the order and write the general solution.

4. (a) Solve :

6

$$\frac{dx}{z(x+y)} = \frac{dy}{z(x-y)} = \frac{dz}{x^2 + y^2}.$$

(b) Solve :

6

$$(y^2 + yz)dx + (xz + z^2)dy + (y^2 - xy)dz = 0.$$

(c) Solve :

6

$$\frac{dx}{dt} + \frac{dy}{dt} + 2x + y = 0,$$

$$\frac{dy}{dt} + 5x + 3y = 0.$$