[This question paper contains 4 printed pages.]

Sr. No. of Question Paper	:	2333	GC-3	Your Roll No
Unique Paper Code	:	62374311		
Name of the Paper	:	Theory of Statist	tical Inferen	ce
Name of the Course	:	B.A. (Program)	STATIST	ICS (CBCS)
Semester	:	III		2
				Manimum Manka : 75

Duration : 3 Hours

Maximum Marks : 75

Instructions for Candidates

- 1. Write your Roll No. on the top immediately on the receipt of this question paper.
- 2. Attempt Six questions in all.
- 3. Q. No. 1 is compulsory. Attempt five more questions.
- 4. Simple calculator can be used.

1. (a) Please identify True/False.

- (i) The Level of Significance is denoted by β .
- (ii) Normal distribution is a particular case of $\chi 2$ Distribution with one d.f.
- (iii) In the case of Poisson Distribution with parameter λ , \bar{x} is Sufficient for λ .
- (iv) If T is consistent estimator of θ , then aT+b is a consistent estimator of $a\theta$ +b.
- (v) Mode of F-Distribution is $n_2 (n_1+2)/n_1(n_2+2)$.
- (vi) A MVUE has a variance that is as small or smaller than the variance of any other unbiased estimator. (1×6)

- (b) Discuss on the following :
 - (i) Null hypothesis and alternate hypothesis.
 - (ii) Mode of F-distribution.
 - (iii) Efficient estimators.
- 2. (a) The manufacturer of television tubes knows from past experience that the average life of tubes is 2,000 hours with a standard deviation of 200 hours. A sample of 100 tubes has an average life of 1,950 hours. Test, at the 0.05 level of significance, if this sample came from a normal population of mean 2,000 hours. State your null and alternative hypothesis and indicate whether a one-tail or two-tail test is used and why? Is the result of the test significant?
 - (b) State and prove Invariance property of consistent estimator. (6,6)
- 3. (a) Find the limiting form of t-distribution for large n.
 - (b) X_1, X_2 and X_3 is a random sample of size 3 from a population with mean value μ and variance σ^2 . T_1, T_2 and T_3 are the estimators used to estimate mean value μ , where

$$T_1 = X_1 + X_2 - X_3, T_2 = 2X_1 + 3X_3 - 4X_2 \text{ and } T_3 = \frac{1}{3}(AX_1 + X_2 + X_3)$$

- (i) Are T_1 and T_2 unbiased estimators ?
- (ii) For which value of A, T, is a consistent estimator?
- (iii) Which is the best estimator ? (6,6)
- 4. (a) Write p.d.f. of χ^2 distribution and also find the moment generating function of χ^2 distribution for n degree of freedom.

(3×3)

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(b) Obtain 100(1-α)% confidence limits (for large samples) for the parameter λ of the poisson distribution :

$$f(x,\lambda) = \frac{e^{-\lambda}\lambda^{x}}{x!}; \qquad x = 0, 1, 2, ...$$
 (6,6)

5. (a) Let p be the probability that a coin will fall head in a single toss in order to test $H_0: p = \frac{1}{2}$ against $H_1: p = \frac{3}{4}$. The coin is tossed 5 times and H_0 is rejected if more than 3 heads are obtained. Find the probability of type I error.

(b) For t-distribution with n degree of freedom, show that :

$$\mu_{2r+1} = 0$$

$$\mu_{2r} = n^{r} \frac{\Gamma\left(\frac{n}{2} - r\right)\Gamma\left(r + \frac{1}{2}\right)}{\Gamma\left(\frac{1}{2}\right)\Gamma\left(\frac{n}{2}\right)}; \quad r = 0, 1, 2, \quad (4,8)$$

and

- 6. (a) Out of 8000 graduates in a town 800 are females; out of 1600 graduate employees 120 are females. Use χ² to determine if any distinction is made in appointment on the basis of sex. Value of χ² at 5% level for one degree of freedom is 3.84.
 - (b) Define MVU estimator. Show that MVU estimator is unique. (6,6)
- (a) Given below are the gain in weights (in kgs.) of pigs fed on two diets A and B.

Diet A:	25	32	30	34	24	14	32	24	30	31	35	25			
Diet B:	44	34	22	10	47	31	40	30	32	35	18	21	35	29	22

Test, if the two diets differ significantly as regards their effect on increase in weight.

- (b) Obtain Cramer-Rao lower bound for the variance of an unbiased estimator θ of normal distribution N(θ , σ^2), where σ^2 is known. (6,6)
- 8. Write short notes on any three of the following :
 - (i) Relation between F and t distribution.
 - (ii) Neyman-Pearson Lemma.

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- (iii) Maximum Likelihood estimator & its Properties.
- (iv) Type I and Type II errors.

(4,4,4)